

# Applications for NLP

## Lecture 5: Linguistics in NLP - 4

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# Outline

## 1 Review

## 2 More Semantics

- Type Theory & Lambda Calculus
- Dynamic Semantics
- Lexical Semantics
- Semantics in NLP

# In The Last Lecture

- Semantics is all about “**meaning**”
  - Lexical Meaning - Lexical Semantics
  - Sentence Meaning - Compositional Semantics
  - Discourse Meaning - Discourse Semantics
- Predicate Logic & First Order Logic, some confusing pairs:
  - Constants and Variables
  - Terms and Formulae
  - Functions and Predicates

# Type Theory

- Church's **Theory of Types**: developed by Alonzo Church, father of **lambda calculus**
- Montague's semantic framework was based on Church's type theory
- Informal Definition (recursive)
  - There is a set of **basic types**  $\{t_1, t_2 \dots t_n\}$
  - If  $x$  and  $y$  are types, then  $x \rightarrow y^1$  is also a type, we call it **complex type**
- In Montague Semantics, two basic types  $e$  and  $t$ 
  - $e$  denotes the type of entities (or individuals)
  - $t$  denotes the type of propositions (or truth values)
  - Other type examples:  $e \rightarrow t$ ,  $(e \rightarrow t) \rightarrow t$ ,  
 $(e \rightarrow t) \rightarrow (e \rightarrow t) \dots$

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<sup>1</sup>Sometimes also denoted as  $\langle x, y \rangle$ .

# Lambda Calculus & Lambda Term

- Lambda Calculus can be viewed as an **extension** of FOL
- $\lambda$  expressions
  - General Form:  $\lambda VAR.\phi$   
VAR stands for **variables**,  $\phi$  stands for **formulas** (not term)
  - Examples:  $\lambda x.P(x)$ ,  $\lambda y.\phi$ ,  $\lambda x.man(x)$
- **Bound/Free** variable: depending on whether VAR appears in the **scope** of the  $\lambda$  operator or not **in the  $\lambda$  term**

## Example (Bound/Free Variables)

Indicate all bound and free variables (if there is any) in the following  $\lambda$  expression:

**1**  $\lambda x.\lambda y.(P(x) \wedge Q(y)) \Rightarrow x, y$  Bound

**2**  $\lambda x.\lambda y.(P(x) \wedge Q(y) \wedge M(z)) \Rightarrow x, y$  Bound,  $z$  Free

**3**  $\lambda x.\lambda y.P(x) \wedge Q(y) \Rightarrow x$  Bound,  $y$  Free

# $\alpha$ -conversion & $\beta$ -reduction

- $\alpha$ -conversion: the **renaming** of bound variables in a  $\lambda$  expression, yielding an equivalent expression
  - $\lambda x.P(x) \Rightarrow_{\alpha} \lambda y.P(y)$
  - $\lambda x.\lambda y.(P(x) \wedge Q(y)) \Rightarrow_{\alpha} \lambda a.\lambda b.(P(a) \wedge Q(b))$
- $\beta$ -reduction: the process that the corresponding variable in the formula is **rewritten** by the argument, until the function itself is reduced to a simpler form
  - $\lambda x.P(x)@y \Rightarrow_{\beta} P(y)$
  - $\lambda x.run(x)@J \Rightarrow_{\beta} run(J)$
  - $\lambda x.\lambda y.(P(x) \wedge Q(y))@a@b \Rightarrow_{\beta}$   
 $\lambda y.(P(a) \wedge Q(y))@b \Rightarrow_{\beta}$   
 $P(a) \wedge Q(b)$

# How To Do Lambda Calculus?

Steps of doing Lambda Calculus:

- 1 Determine which expression is the **function** and which is the **argument**
- 2 Apply the argument to the function
- 3  $\beta$ -**reduce** the conjoined element

## Example ( $\lambda$ Calculus)

$$\lambda P.\lambda x.(P(x) \wedge \text{good}(x)) @ \lambda x.\text{man}(x) \Rightarrow_{\alpha}$$

$$\lambda P.\lambda x.(P(x) \wedge \text{good}(x)) @ \lambda y.\text{man}(y) \Rightarrow_{\beta}$$

$$\lambda x.(\lambda y.\text{man}(y) @ x \wedge \text{good}(x)) \Rightarrow_{\beta}$$

$$\lambda x.(\lambda y.\text{man}(y) @ x \wedge \text{good}(x)) \Rightarrow_{\beta}$$

$$\lambda x.(\text{man}(x) \wedge \text{good}(x))$$

# Semantics Exercise

## Question

Compute the result for the following Lambda Calculus:

- $\lambda x.x@y$
- $\lambda x.y@y$
- $\lambda x.P(x) \wedge Q(y)@y$
- $\lambda x.y.P(x) \wedge Q(y)@y@z$
- $\lambda x.xy@(\lambda z.zy)$
- $\lambda x.xx@ \lambda x.xx$



## Semantics Exercise

## Answer

Compute the result for the following Lambda Calculus:

- $\lambda x.x@y \Rightarrow_{\alpha,\beta} y$
- $\lambda x.y@y \Rightarrow_{\alpha,\beta} y$
- $\lambda x.P(x) \wedge Q(y)@y \Rightarrow_{\alpha,\beta} P(y) \wedge Q(z)$
- $\lambda x.y.P(x) \wedge Q(y)@y@z \Rightarrow_{\alpha,\beta} P(y) \wedge Q(z)$
- $\lambda x.xy@(\lambda z.zy) \Rightarrow_{\alpha,\beta} yx$
- $\lambda x.xx@ \lambda x.xx \Rightarrow_{\alpha,\beta} \lambda x.xx$

# Typed Lambda Calculus

- Definition: in **Typed Lambda Calculus**, everything (variable, constant or predicate) in the  $\lambda$  expression has its type
- For a **predicate** relation (function-argument), types are strictly restricted
  - The type of the predicate and the type of the argument(s) **must** match
  - Example:  $xy/x@y \rightarrow y(t_1), x(t_1 \rightarrow t_2), xy/x@y(t_2)$
  - As a result, “ $\lambda x.xx$ ” is prohibited in Typed Lambda Calculus, the formula “ $xx$ ” is not typeable

# Types & Syntactic Categories

Every syntactic category has its own type

## ■ Common Nouns

- Example:  $\lambda x.man(x)$ ,  $\lambda x.car(x)$
- Type:  $e \rightarrow t$
- The **property** of being an  $x$  such that  $x$  is a man

## ■ Determiners

- Example:  $\lambda PQ.\exists x.(P(x) \wedge Q(x))$ ,  $\lambda PQ.\forall x.(P(x) \rightarrow Q(x))$
- Type:  $(e \rightarrow t) \rightarrow ((e \rightarrow t) \rightarrow t)$

## ■ Noun Phrases

- Example:  $\lambda Q.\exists x.(man(x) \wedge Q(x))$ ,  $\lambda Q.\forall x.(man(x) \rightarrow Q(x))$
- Type:  $(e \rightarrow t) \rightarrow t$

# Types & Syntactic Categories

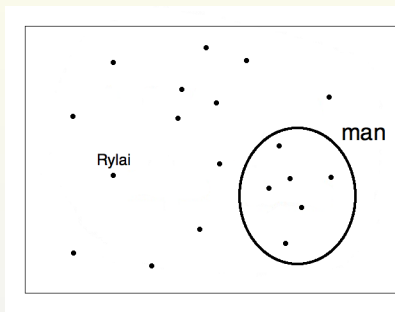
- Proper Names
  - Example: *RYLAI*, *LINA* or  $\lambda P.P(RYLAI)$ ,  $\lambda P.P(LINA)$
  - Type:  $e$  or  $(e \rightarrow t) \rightarrow t$
- Intransitive Verb (similar to Common Noun)
  - Example:  $\lambda x.run(x)$ ,  $\lambda x.sleep(x)$
  - Type:  $e \rightarrow t$
- Transitive Verb
  - Example:  $\lambda OS.S(\lambda x.(O\lambda y.love(x, y)))$
  - Type:  $((e \rightarrow t) \rightarrow t) \rightarrow (((e \rightarrow t) \rightarrow t) \rightarrow t)$
- Adjective<sup>2</sup>
  - Example:  $\lambda Px.(P(x) \wedge red(x))$
  - Type:  $(e \rightarrow t) \rightarrow (e \rightarrow t)$

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<sup>2</sup>The  $\lambda$  expression for adjectives is a complicated problem, here I just give a simple example.

# Some Deeper Questions About Types

- Why common nouns are of type “ $e \rightarrow t$ ”? ( $\lambda x.man(x)$ )
  - In natural language, common nouns are properties, or sets
  - $\lambda x.man(x)$  denotes the set of “man” or the properties that every “man” shares in common
- How about Proper Names?
  - Take it as a constant (*RYLAI*)
  - $(e \rightarrow t) \rightarrow t$ : set of sets, or set of properties
  - The properties that the entity possesses ( $\lambda P.P(RYLAI)$ )
- NPs? Intransitive Verbs?



# Compositionality

## Frege's Principle (Compositionality)

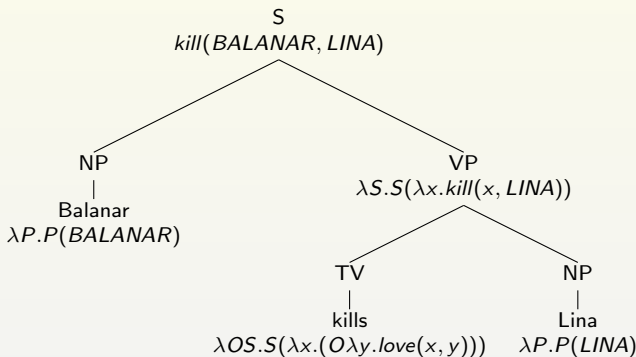
The meaning of a complex expression is determined by the meanings of its constituents and the structure they are combined.

## Montague Semantics

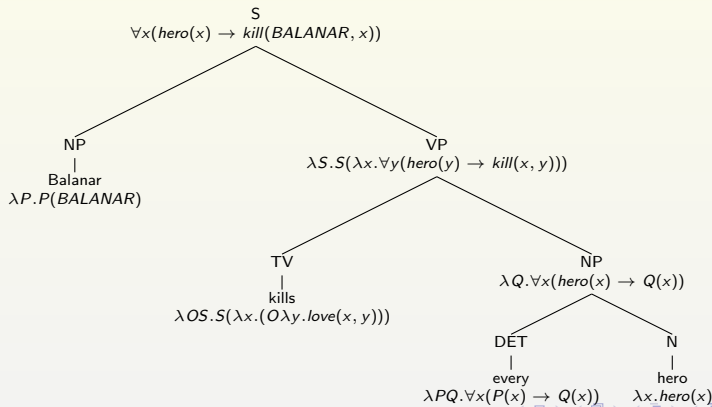
Type Theory + Lambda Calculus + First Order Logic (FOL) + Compositionality

# Doing Semantics Compositionally

*Balanar kills Lina.*



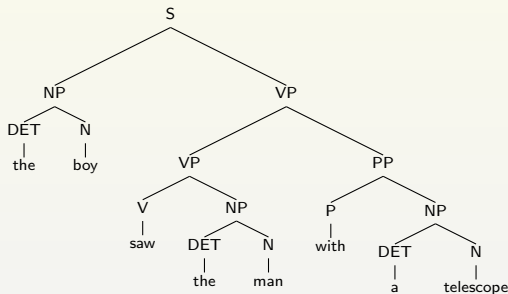
## Doing Semantics Compositionally

*Balanar kills every hero.*



# Syntactic Ambiguity

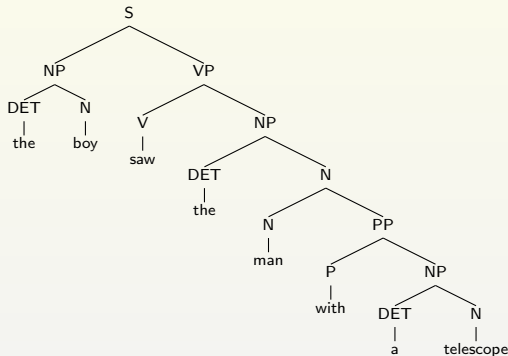
- Definition: the same sequence of words is interpreted as having different **syntactic structures**
- Examples
  - *The boy saw the man with a telescope.*



# Syntactic Ambiguity Continued

## ■ Examples

- *The boy saw the man with a telescope.*



# Semantic Ambiguity

- Definition: with the same **syntactic structure**, there exists different **meaning interpretations**
- *Every man loves a woman.*
  - 1 There is a celebrity woman, and every man in the world likes her
  - 2 For every man in the world, there is a woman that he likes
- Meaning representation for the two readings
  - 1  $\exists y(woman(y) \wedge \forall x(man(x) \rightarrow love(x, y)))$
  - 2  $\forall x(man(x) \rightarrow \exists y(woman(y) \wedge love(x, y)))$
- How to resolve scope ambiguity?
  - Two alternative syntactic structures<sup>3</sup>
  - Cooper Storage: computationally expensive

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<sup>3</sup>This solution is not general enough because it is not practical to assign every sentence two structures

# Where Compositional FOL Fails?

## 1 *A hero dies. He revives at the fountain.*

- What is the FOL translation?
  - $\exists x(\text{hero}(x) \wedge \text{die}(x)) + \text{revive}(x) ???$
  - $\exists x(\text{hero}(x) \wedge \text{die}(x) \wedge \text{revive}(x))$
- Scope of “ $\exists x$ ” is extended, **not** a systematic solution

## 2 *Every farmer who owns a donkey beats it.*

- What is the FOL translation of this sentence?
  - $\forall x(\text{farmer}(x) \wedge \exists y(\text{donkey}(y) \wedge \text{own}(x, y)) \rightarrow \text{beat}(x, y)) ???$
  - $\forall x \exists y(\text{farmer}(x) \wedge \text{donkey}(y) \wedge \text{own}(x, y) \rightarrow \text{beat}(x, y)) ???$
  - $\forall x \forall y(\text{farmer}(x) \wedge \text{donkey}(y) \wedge \text{own}(x, y) \rightarrow \text{beat}(x, y))$
- Same meaning as “*if a farmer owns a donkey, then he beats it.*”
- Why **existential** quantifier “*a*” should be translated into **universal** quantifier?

# Dynamic Semantics

- **Dynamic Semantics**
  - Why dynamic - pieces of text or discourse are viewed as instructions to **update** an existing context with new information
  - In a slogan - **meaning is of context change potential**
- Other dynamic semantic formalisms
  - **File Change Semantics** by Irene Heim
  - **Dynamic Predicate Logic** by Groenendijk & Stokhof
  - **Dynamic Treatment to MS** by Philippe de Groote<sup>4</sup>

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<sup>4</sup>More information refers to the paper "Towards a Montagovian account of dynamics"

# Motivation for “Event”

In Davidson’s 1967 paper “The Logical Form of Action Sentences”, **event** was described as a **linguistic entity** in action sentences

- Modifiers

- Examples:

- 1 *Brutus stabbed Caesar in the back with a knife.*

- 2 *Brutus stabbed Caesar in the back.*

- 3 *Brutus stabbed Caesar with a knife.*

- 4 *Brutus stabbed Caesar.*

- How to represent meanings of the 4 sentence in a logical way, while pertaining the entailment relation among them?

- Higher Order Modifiers

- Multiple Predicates:  $stab_1, stab_2, stab_3$

- A “Complete” Predicate:  $stab(subj, obj, location, tool...)$

- **Event**

# Motivation for “Event” Continued

## ■ Modifiers

### ■ Representation with Event

1  $\exists e(stab(e) \wedge subj(e, B) \wedge obj(e, C) \wedge in(e, back) \wedge with(e, knife))$

2  $\exists e(stab(e) \wedge subj(e, B) \wedge obj(e, C) \wedge in(e, back))$

3  $\exists e(stab(e) \wedge subj(e, B) \wedge obj(e, C) \wedge with(e, knife))$

4  $\exists e(stab(e) \wedge subj(e, B) \wedge obj(e, C))$

■ Implication Result:  $S_1 \rightarrow S_2 \rightarrow S_4, S_1 \rightarrow S_3 \rightarrow S_4$

## ■ Vague Semantic Ambiguities

### ■ Examples:

■ *John and Mary went to school.*

■ *John loves all women he meets.*

■ How many “events” are there?

## ■ “Event” Everywhere

■ *I'll sleep after **that**.*

■ *I'll do **that** first.*

# Verb Classification 1

## ■ Intuitional Way

- **Main Verb** (Action Verb): a verb that is used to describe an action or an event
  - Intransitive verb, transitive verb, di-transitive verb...
  - Example: *run, play, give...*
- **Auxiliary Verb**: a verb that does not have a real meaning by itself, while it requires to go along with another action verb
  - Expressing tense, passiveness, modality
  - Examples: *have, be, could, should...*
- **Linking Verb** (State Verb): a verb that denotes the state of the object
  - Has meaning, but can not describe an action or event
  - Example: *seem, smell, be...*



# Verb Classification 2

- Vendler's Way<sup>5</sup>
  - **State Verb**: no effect of meaning changing or modifying during the time span
    - Example: *John loves Mary. John is tall.*
  - **Activity Verb**: describing a concrete on-going action, that has internal change and duration, but end point is not necessary
    - Example: *John runs. John walks along the river.*
  - **Achievement Verb**: besides describing an event or action, an end point or culmination is required, the event should be without duration
    - Example: *Mary arrived at the destination. John reaches the top of the mountain*
  - **Accomplishment Verb**: nearly the same as the achievement verb except that the described event needs to have duration
    - Example: *John consumed an apple.*

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<sup>5</sup>This classification is based on Vendler's 1967 paper "Verbs and Times".

# Thematic Roles

- What is “Thematic Role”?
  - View the verb as the **center** of the sentence, the **roles** that the rest parts of the sentence play
  - Coarse Example: subject, object, location...
- Why we need “Thematic Role”?
  - Assumption: languages do not differ in expressive power
  - A **universal representation** at the semantic level
- Examples
  - *Brutus (**Agent**) stabbed Caesar (**Theme**) with a knife (**Instrument**).*
  - *Caesar (**Theme**) was stabbed by Brutus (**Agent**) with a knife (**Instrument**).*
- Thematic Roles do not change with sentence structures

# Thematic Roles Details

- It is still **controversial** to declare how many thematic roles are there
- A general framework

Thematic Role	Syntactic Correspondence
Agent	Subject
Theme	Direct object; subject of “be”
Goal	Indirect object, or with “to”
Benefactive	Indirect object, or with “for”
Instrument	Object of “with”; subject
Experiencer	Subject

# Semantics in NLP - WSD

- Word Sense Disambiguation
  - A word could have **several** meanings
  - Disambiguation between different meanings is necessary
  - Needed for most NLP that involve semantics
  - Selectional restrictions to identify meanings intended in given context
    - 1 *The astronomer saw **the star**.*
    - 2 *The astronomer married **the star**.*
  - Statistical evidence derived from large corpora
    - 1 *John sat on **the bank**.*
    - 2 *John went to **the bank**.*
    - 3 *King Kong sat on **the bank**.*

# Semantics in NLP -LR

## ■ Lexical Relations

- **Relations** among word meanings are also very important for natural language based applications
- The most commonly used lexical relations
  - **Hyponymy** (is\_a) e.g., *dog* is a hyponym of *animal*, *animal* is the hypernym of *dog*
  - **Meronymy** (part-of) e.g., *arm* is a meronym of *body*
  - **Synonymy** e.g., *eggplant* & *aubergine*, *fall* & *autumn*
  - **Antonymy** e.g., *big* & *little*, *tall* & *short*
- **WordNet**: a good source for lexical relations

# Semantics in NLP - LR Continued

- In natural language applications, the most commonly used lexical relation is hyponymy such that
  - **Semantic Classification** (e.g., selectional restrictions, named entity recognition)
  - **Shallow Inference** (e.g., “*X murdered Y*” implies “*X killed Y*”)
  - **Word Sense Disambiguation**
  - **Machine Translation** (if a term cannot be translated, substitute a hypernym)

# Semantics in NLP - Other

- **Shallow** Semantic Parsing (Role Labeling)
  - Based on the event structure, labeling the thematic roles of each components
  - Potential Situations
    - Historical document
    - Newspaper, live sport commentary (football, basketball)
- Natural Language **Understanding**
  - Ultimate goal for NLP
  - Same words, different meanings
    - 1 *John loves Mary.*  $\Rightarrow$  *love*(J, M)
    - 2 *Mary loves John.*  $\Rightarrow$  *love*(M, J)

# Summary

- Type Theory & Lambda Calculus
- Typed Lambda Calculus and natural language semantics
- Compositional Semantics - obtaining meaning representation in a systematic way
- Dynamic Semantics
- Event Semantics & Thematic Roles
- Semantics in NLP applications